

# FEM Analyses on Seismic Responses of Rocking Structural Systems with Yielding Base Plates

by

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## ABSTRACT

The seismic responses of the base-plate-yielding rocking systems are examined by the finite element analysis. A three-story, one-by-two bay braced steel frame of two-thirds scale is analyzed, that was previously tested by a shaking table. The total height of the frame is 5.3 meters and the total weight is 15.6 tons. The yielding base plates are installed at the bottom of each column at the first story of the frame. The earthquake ground motion used for the analyses is the record of the 1940 El Centro NS component whose time scale is shortened to  $1/\sqrt{2}$ . From the analytical results, it is concluded that the seismic responses of the base-plate-yielding rocking systems are appropriately simulated comparing with the experimental results obtained from the previous shaking table tests.

**KEYWORDS:** Seismic Response Analysis, Finite Element Method, Seismic Response Reduction, Rocking Vibration, Up-lift, Base Plate Yielding

## 1. INTRODUCTION

It has been pointed out that the effects of rocking vibration (up-lift response) may reduce the seismic damage of buildings subjected to strong earthquake ground motions [1, 2]. Based on these experiences, the rocking structural systems have been developed that cause rocking vibration under appropriate control during major earthquake ground motions [3, 4].

One of the rocking structural systems under development has yielding base plates at the bottom of each steel column of the lowest story. When the weak base plates yield due to tension of column during a strong earthquake ground motion, a building structure causes rocking vibration. The basic idea of the base plate

yielding systems is illustrated in Fig. 1.

In this paper, the seismic responses of the base-plate-yielding rocking systems are examined by the finite element analysis [5] comparing with the experimental results obtained from the previous shaking table tests [3, 4].

## 2. TEST FRAME AND EXPERIMENTAL PROCEDURES

The experimental results of the previous shaking table tests on the base-plate-yielding rocking systems are briefly summarized below, whose details are published elsewhere [3, 4].

A three-story, one-by-two bay braced steel frame of two-thirds scale was tested on a large shaking table in Tsukuba. The test frame is composed of moment-resisting steel frames and structural components such as yielding base plates installed to the bases of the columns at the first story and bracing members of high-strength prestressing steel bar as shown in Figs. 2 and 3. The total height of the frame is 5.3 meters, each floor height is 1.7 meters at the first story and 1.8 meters at the second and third stories, each floor plan is 3 by 4 meters, and the total weight is 15.6 tons. The span is 3 meters in the test direction. The mass of each floor and the cross sections of members are shown in Tables 1 and 2, respectively.

The yielding base plates are installed at the

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bottom of each column at the first story of the test frame as shown in Fig. 3. Two types of base plates with different strength are used in the test. The thickness of the base plates is 6 mm and 9 mm. Mechanical characteristics of steel base plates are listed in Table 3. The test frame with base plate thickness of 6 mm is referred to as BP6 model, the test frame with that of 9 mm referred to as BP9 model, respectively. The base plate of BP6 and BP9 models has four wings that are 100 mm in length and 100 mm in width. The test frame with base plate of two wings is referred to as BP9-2 model.

The test frame was tested in one horizontal direction, which coincides with the strong axis of each column.

The earthquake ground motion used for the tests was the record of the 1940 El Centro NS component whose time scale was shortened to  $1/\sqrt{2}$ . The maximum input acceleration was adjusted in several levels to examine the responses of each test frame.

### 3. ANALYTICAL MODELING AND NUMERICAL ANALYSIS

#### 3.1 Analytical Model and Assumptions

The mathematical idealization of the test frame is illustrated in Fig. 4. One of the three frames in the test direction is modeled as shown in Fig. 4(a). The base plates and the columns of the first story are modeled as shell elements as shown in Fig. 4(b). The columns and girders at the second and third stories are modeled as beam elements, and the bracing members as truss elements.

The base plates are assumed to be elasto-plastic materials considering the finite deformation, for which the kinematic hardening rule is applied and the shear strain energy theory is used as the yield condition. The other elements are assumed to be elastic. The bracing members are assumed to resist only tensile force, in which the initial strain of  $1050 \mu$  is applied. The foundation beam is assumed to be rigid.

The nodal points along the edge of the restraint steel plate are fixed as shown in Fig. 4(b). The

rigid connection is assumed between shell and beam elements at Point B in Fig. 4(a). The out-of-plane displacements are restrained at the beam-to-column connections at the roof level.

#### 3.2 Numerical Analysis

The masses of the frame model based on the actual dead loads of the test frame are lumped at each nodal point. The vertical dead loads that correspond to the lumped masses are applied statically to each node of the frame model before starting the dynamic response analysis.

It is assumed that the viscous damping results from the initial stiffness-dependent effects. The critical damping ratio of 0.5% is introduced to the first mode in bending, whose value is compatible with the shaking table test results of the test frame [3, 4].

The numerical time integration in the analysis is the combined use of the Newmark method with integration constant equal to  $1/4$  based on the constant acceleration and the Newton-Raphson method of equilibrium iteration within the time step of 0.001 second.

The measured accelerogram on the shaking table in the shaking table tests [3, 4] is used in the dynamic response analysis of the frame model, which is the record of the 1940 El Centro NS component whose time scale is reduced to  $1/\sqrt{2}$ . The duration time is six seconds in the analysis.

### 4. Analytical Results and Discussion

The analytical results in the case of BP9-2 model (base plate of two wings) subjected to the maximum acceleration of  $6.02 \text{ m/s}^2$  in the shaking table tests [3, 4] are presented and discussed in this chapter.

#### 4.1 Mode Shapes and Natural Periods

The translational vibration mode shapes in the first and second bending modes are illustrated in Fig. 5. The natural periods of the first and second bending modes of the rocking frame model are 0.260 s and 0.066 s respectively, and those of the fixed-base frame model are 0.160 s and 0.056 s respectively.

#### 4.2 Time History Responses

The time history of the roof displacement response at Point C in Fig. 4(a) is shown in Fig. 6. The translational vibration period is close to the natural period of the first bending mode of the rocking frame model that is 0.260 s. The maximum roof displacement from the analytical results agrees approximately with that from the test results. The analytical results correspond very well to the test results.

The time history of the up-lift displacement response at the center of the base plate on the west side is shown in Fig. 7. The analytical results simulate quite well the test results. The up-lift motion in the analysis occurs alternately between the west and east sides as observed in the shaking table tests. The maximum up-lift displacement is about 12.5 mm in the analysis, while it is about 10 mm in the test.

The time history of the change of axial force of the east column at the first story is shown in Fig. 8. The large impact force in compression is observed approximately in the instant when the base plate touches down. The maximum change of compressive force in the analysis is 0.8 times as much as that in the test. The reason may be that the viscous damping is assumed to be initial stiffness dependent in the analysis, so that the response in the higher modes such as the longitudinal vibration mode of the column is suppressed.

#### 4.3 Local Behavior

Fig. 9 illustrates the strain distribution on the bottom surface of the west base plate in the oscillation direction at the time of 5.07 s when the up-lift displacement reaches the maximum. The maximum local strain close to the fixed nodal points of the base plate, at Point D in Fig. 9, goes up to 18800  $\mu$  in tension, which exceeds the yield point of steel but is far away from the fracture strain. The peak local strain near the column end of the base plate, at Point E in Fig. 9, attains to 6800  $\mu$  in compression.

Fig. 10 illustrates the strain distribution on the surface of the bottom of the west column at the

first story in the longitudinal direction at the time of 5.28 s when the axial strain reaches the maximum in compression. At this time, the peak local strain in compression at Point F in Fig. 10 goes up to 1100  $\mu$ , which does not attain to the yield point of steel. As a result, the local buckling never occurs in the steel plate elements of the column

## 5. CONCLUSIONS

The seismic responses of the base-plate-yielding rocking systems are studied by the finite element analysis by comparison with the experimental results obtained from the previous shaking table tests. It is concluded that the results of the numerical simulation harmonizes quite well with the test results in not only the overall responses but also the local behavior.

## 6. ACKNOWLEDGMENTS

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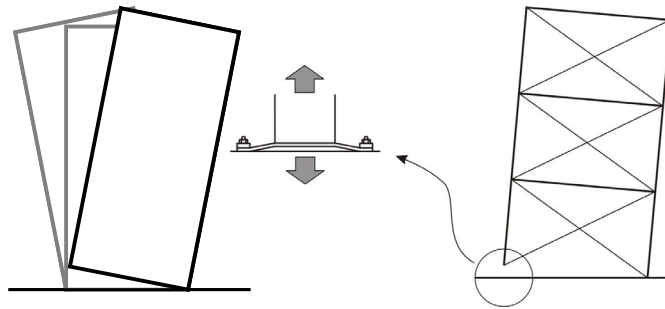
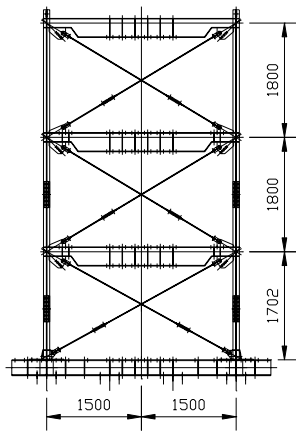
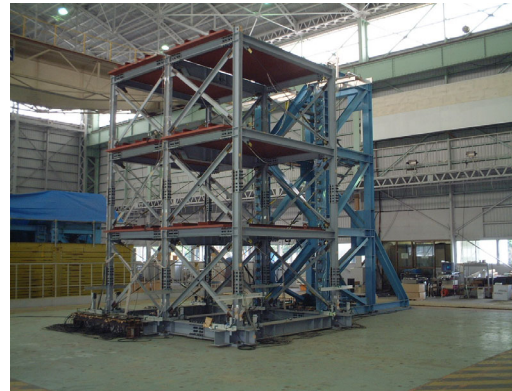


Fig. 1 Structural Rocking System with Yielding Base Plates.



(a) Elevation



(b) Overall View

Fig. 2 Test Frame

Table 1 Mass of Floor

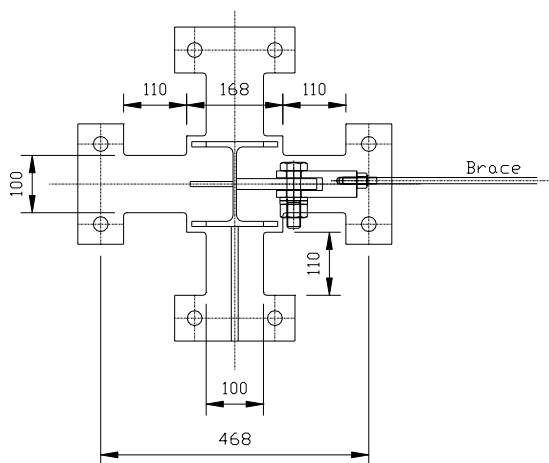
Floor	Mass (t)
Roof	4.6
3	5.2
2	5.2

Table 2 Member Cross Sections

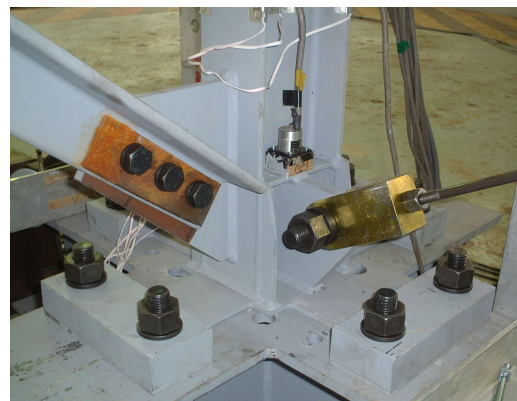
Member	Size (mm)
Column	H-148x100x6x9
Beam	H-150x150x7x10
Brace	$\phi$ -11

Table 3. Mechanical Characteristics of Steels

Model	JIS	Yield point (MPa)
BP6	SS400	330
BP9	SS400	292



(a) Plan



(b) Close-up View

Fig. 3 Yielding Base Plate

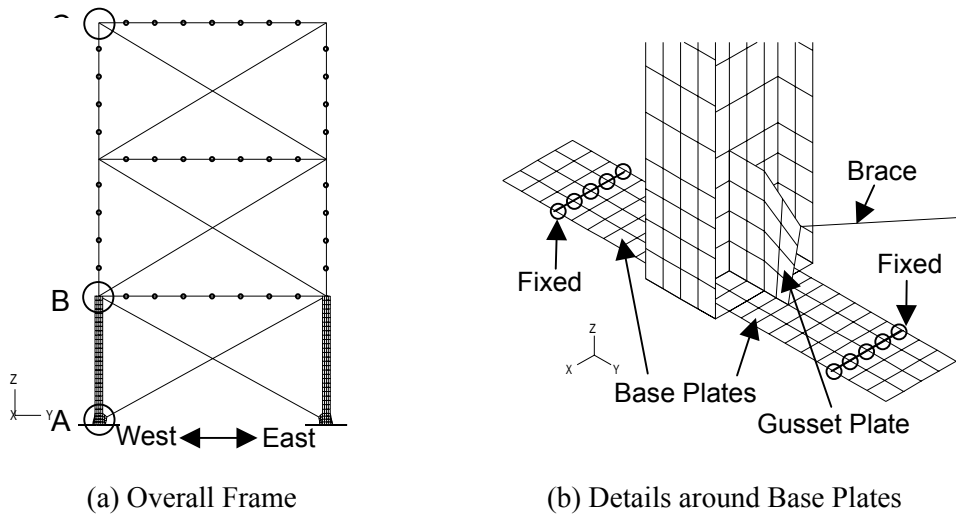


Fig. 4 Finite Element Analytical Model

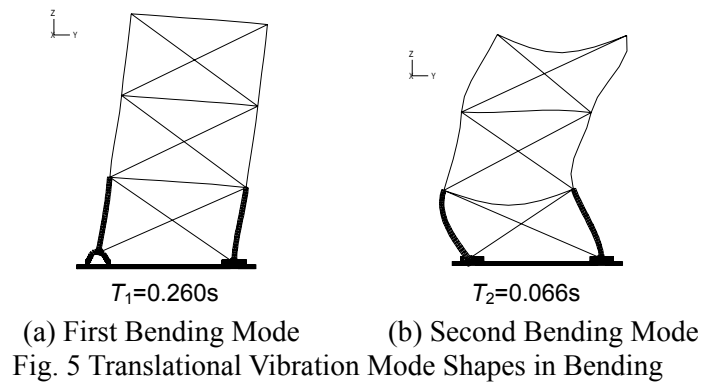


Fig. 5 Translational Vibration Mode Shapes in Bending

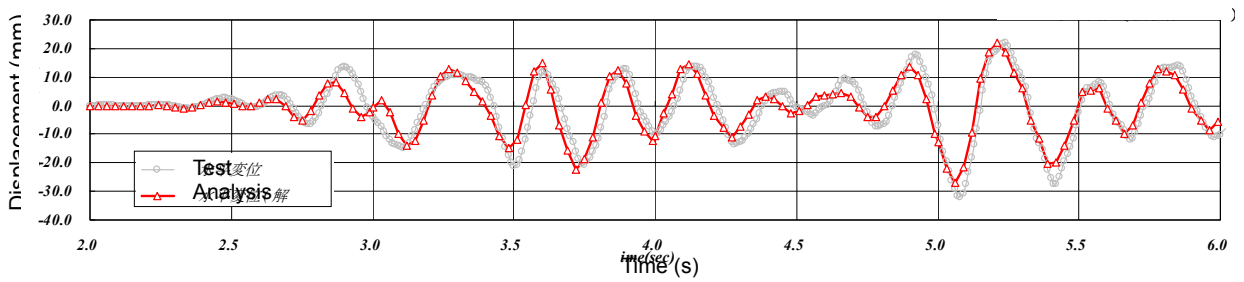


Fig. 6 Time History of Roof Displacement Response of BP9-2 Model: max. input acc.=6.02m/s<sup>2</sup>

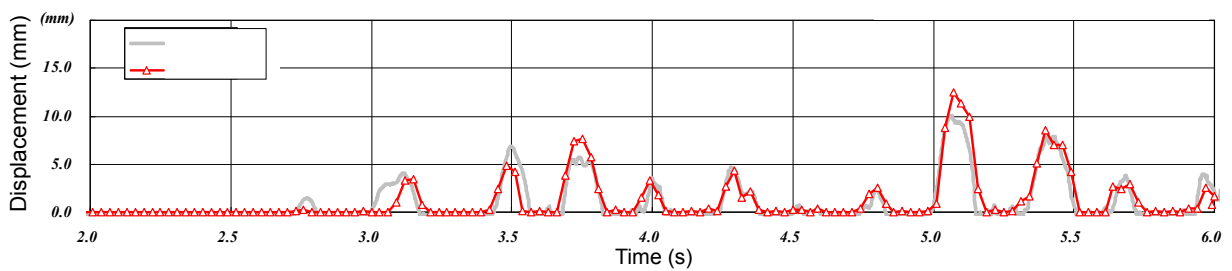


Fig. 7 Time History of Up-lift Displacement Response at Base Plate: max. input acc.=6.02m/s<sup>2</sup>

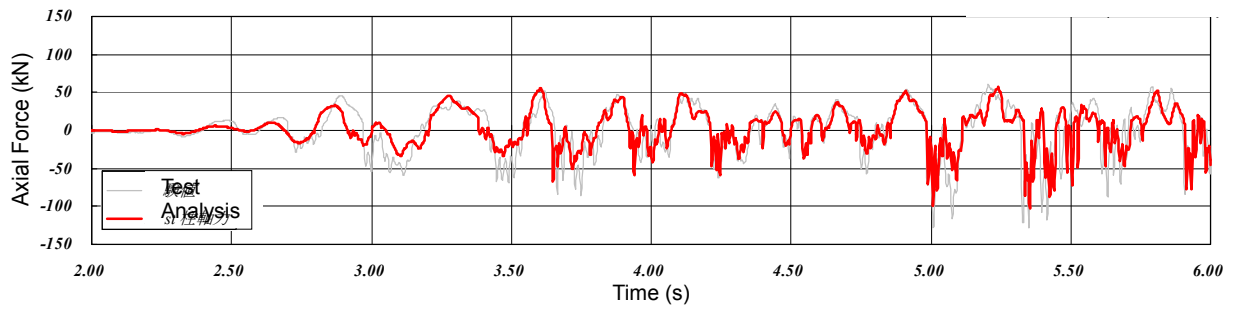


Fig. 8 Time History of Axial Force Change of East Column at 1st Story: max. input acc.=6.02m/s<sup>2</sup>

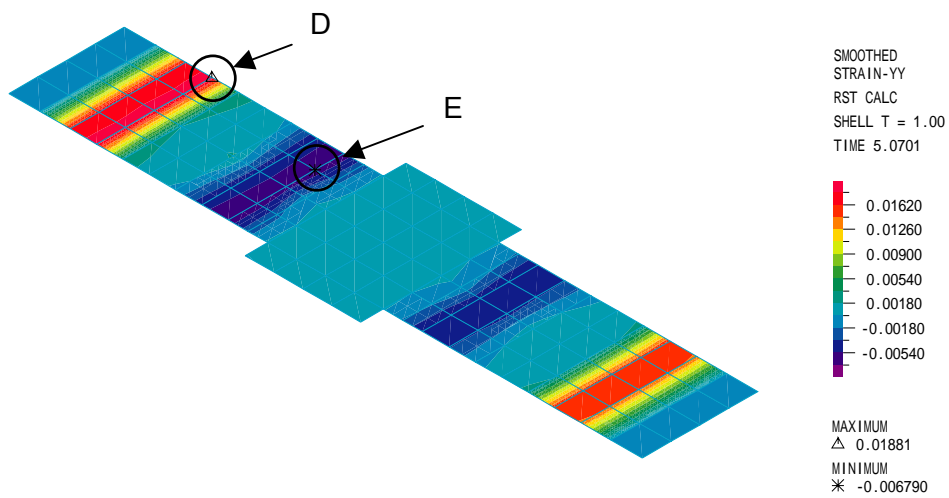


Fig. 9 Strain Distribution on Bottom Surface of West Base Plate in Oscillation Direction (t=5.07s)

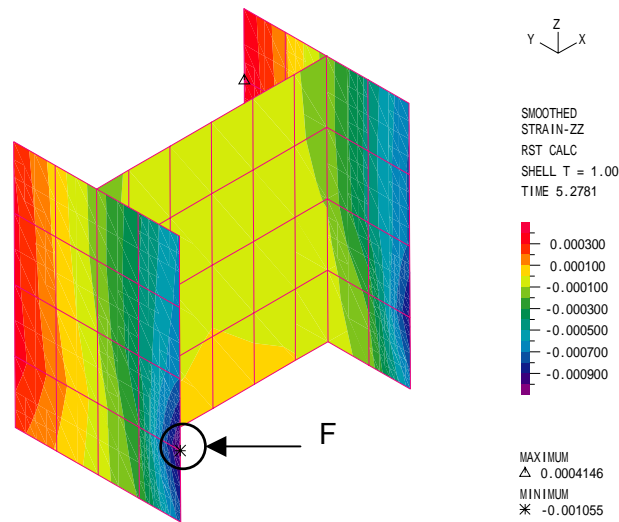


Fig. 10 Strain Distribution on Surface of Bottom of West Column in Longitudinal Direction (t=5.28s)